

# Ideal Gas Thermodynamic Functions of the Isotopic Hydrogen Cyanides<sup>1</sup>

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The ideal gas thermodynamic functions for HCN, DCN, and TCN were calculated from molecular data. The recent spectroscopic data for HCN and DCN by Allen [1]<sup>3</sup> and Douglas and Sharma [2] were employed. The zero frequencies of TCN were obtained by a normal coordinate treatment. The partition functions are obtained in closed form. The calculations include high-temperature corrections for vibrational anharmonicity, rotation-vibration coupling, centrifugal stretching, and azimuthal quantum effects, and low-temperature corrections for nonclassical rotation. The statistical calculations were performed on the Standards Electronic Automatic Computer (SEAC). Tables of  $C_p/R$ ,  $(H^\circ - E_0^\circ)/RT$ ,  $-(F^\circ - E_0^\circ)/RT$ , and  $S^\circ/R$  have been calculated at small temperature intervals from 50° to 5,000° K.

## 1. Introduction

The procedure developed in earlier papers [3,4,5] for high-speed machine computation of the thermodynamic functions of molecules in the ideal gas state was used. The partition function is written in a factored form to include corrections for vibrational anharmonicity, rotation-vibration coupling, centrifugal stretching, nonclassical rotation, and azimuthal quantum effects. The expression for the factored internal partition function is

$$Q = \frac{1}{S} \left[ \prod_i (1 - e^{-u_i})^{d_i} \right] \left[ \frac{kT}{hcB_e} \right] \left[ 1 + \rho T \right] \left[ \prod_i \left( 1 + \frac{d_i \delta_i}{e^{u_i} - 1} \right) \right] \left[ \prod_{i \leq j} (1 + f_{ij}) \right] \left[ 1 + \frac{\theta_1}{T} + \frac{\theta_2}{T^2} \right]$$

where

$$\rho = (2kD)/hcB_e^2,$$

$$\theta_1 = \frac{1}{3} (hcB_e)/k, \theta_2 = \frac{1}{15} (hcB_e/k)^2$$

and

$$f_{ij} = \frac{d_i(d_j + \delta_{ij})X'_{ij}(hc/kT)}{(e^{u_i} - 1)(e^{u_j} - 1)}, X'_{ij} = X_{ij} + g_{ij}/3.$$

In these expressions the  $\delta_i$  represent rotation-vibration coupling constants, the  $X_{ij}$  are the anharmonic constants,  $g_{22}$  is an anharmonic constant for the doubly degenerate vibration,  $\omega_2$ , and  $\delta_{ij}$  is the Kronecker delta. Pennington and Kobe's method [6] of including the  $g_{22}$  term in the partition function was used. The other symbols and constants have their usual meaning (see e. g., [3]).

## 2. Molecular Data

The vibrational data for HCN and DCN were recently obtained by Allen [1]. The rotational data for HCN and DCN were investigated by Douglas and Sharma [2]. The anharmonicity and rotation-vibration coupling constants were calculated for TCN using the isotope relations [3],

$$X'_{ij} = \left( \frac{\omega'_i \omega'_j}{\omega_i \omega_j} \right) X_{ij} \quad \text{and} \quad \delta'_i = \left( \frac{\omega'_i}{\omega_i} \right) \delta_i$$

where the primed quantities refer to the molecule whose  $X_{ij}$  or  $\delta_i$  is to be calculated, and the unprimed quantities refer to the reference molecule. The  $X_{ij}$  and  $\delta_i$  for TCN were calculated using HCN and DCN as reference molecules; the averages of these calculations were used in the tabulated results except for the constant  $X_{12}$  in which case DCN was used as a reference molecule. Approximating

$$f_{ij} = \frac{d_i(d_j + \delta_{ij}) \frac{hc}{kT} X'_{ij}}{(e^{u_i} - 1)(e^{u_j} - 1)} \quad \text{by} \quad f_{ij} = \frac{d_i(d_j + \delta_{ij}) \frac{hc}{kT} X'_{ij}}{(e^{u_k} - 1)^2}$$

where  $u_k = u_i u_j$  changes the correction factor  $f_{23}$  by 20 percent and the free energy by 1 part in 36,000 at 5,000°K. This effect is much less in the case of  $f_{13}$  and  $f_{12}$  (see [3]). The zero-order frequencies for TCN were obtained by a normal coordinate treatment.

The chemical atomic weights used in the calculations of the translational partition functions were obtained from the values listed by Wichers [7]. The isotopic mass used in the zero-point frequency and equilibrium moment of inertia calculation are listed by Mattauch and Fluegge [8]. The constants used are given in table 1.

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<sup>3</sup> Figures in brackets indicate the literature references at the end of this paper.

TABLE 1. Molecular constants

	Units	HCN	DCN	TCN
$\nu_1$	cm <sup>-1</sup>	2100.24	1927.27	1723.90
$\nu_2$	cm <sup>-1</sup>	711.90	569.13	503.36
$\nu_3$	cm <sup>-1</sup>	3315.03	2632.33	2446.67
$X_{11}$	cm <sup>-1</sup>	10.45	7.10	6.37
$X_{22}$	cm <sup>-1</sup>	2.50	2.09	1.45
$X_{33}$	cm <sup>-1</sup>	52.50	20.23	22.72
$X_{12}$	cm <sup>-1</sup>	2.90	-2.73	-1.93
$X_{13}$	cm <sup>-1</sup>	14.43	32.88	18.00
$X_{23}$	cm <sup>-1</sup>	19.19	15.71	11.48
$g_{22}$	dimensionless	3.63	-2.00	-1.00
$\delta_1$	dimensionless	0.00643	0.00518	0.00495
$\delta_2$	dimensionless	-0.0024	-0.0035	-0.0024
$\delta_3$	dimensionless	0.00727	0.00854	0.0066
$I_e$	g cm <sup>2</sup> × 10 <sup>-40</sup>	18.846	23.093	27.029
$\theta_1$	°K	0.7122	0.5812	0.4967
$\theta_2$	(°K) <sup>2</sup>	0.2965	0.1975	0.1442
$\rho$	(°K) <sup>-1</sup> × 10 <sup>-6</sup>	1.79	1.99	1.88

### 3. Thermal Functions

The heat capacity, enthalpy, free energy, and entropy of HCN, DCN, and TCN are listed in tables 2, 3, and 4. The thermal functions are tabulated in dimensionless units at small intervals ranging from 50° to 5,000° K. These tables also include the first differences for the tabulated thermodynamic functions.

The uncertainty in the calculated vibrational anharmonicity and rotation-vibration coupling constants is approximately 25 percent except in the case of the anharmonic constant  $X_{12}$  for TCN in which case the sign of the constant cannot be satisfactorily predicted. The uncertainty in the vibrational and rotational fundamentals is less than 1 percent assuming negligible uncertainty in the calculated zero point vibrational frequencies. At temperatures below 1,000° K this will result in an uncertainty in the third place to the right of the decimal for the tabulated properties of these substances. The thermal functions are tabulated with more figures to permit intercomparison among the several isotopic modifications.

The contribution of the excited electronic states, significant only at the highest temperatures, have been neglected. The entropy contribution of isotopic spin and the entropy of isotopic mixing have been omitted.

Stamm, Halverson, and Whalen [9] have revised older tables of free energy for HCN which include corrections for vibrational anharmonicity, rotation-vibration coupling, centrifugal stretching, and a low-temperature correction. The results reported here are in excellent agreement with those of Stamm et al.

TABLE 2. Ideal gas thermodynamic functions for HCN

°K	$\frac{C_p^\circ}{R}$		$\frac{(H^\circ - E_0^\circ)}{RT}$		$\frac{-(F^\circ - E_0^\circ)}{RT}$		$\frac{S^\circ}{R}$
50	3.50020	4	3.48581	240	14.22796	63576	17.71377
60	3.50025	19	3.48821	173	14.86372	53784	18.35194
70	3.50045	74	3.48994	135	15.40157	46610	18.89152
80	3.50120	209	3.49129	119	15.86768	41128	19.35898
90	3.50329	456	3.49249	128	16.27897	36803	19.77146
100	3.50786	825	3.49378	162	16.64700	33306	20.14078
110	3.51612	1301	3.49540	223	16.98007	30423	20.47547
120	3.52913	1850	3.49763	309	17.28430	28007	20.78193
130	3.54764	2431	3.50073	418	17.56437	25957	21.06511
140	3.57195	3034	3.50491	543	17.82395	24199	21.32887
150	3.60199	3539	3.51035	680	18.06595	22676	21.57630
160	3.63739	4013	3.51716	823	18.29271	21346	21.80987
170	3.67753	4415	3.52539	966	18.50618	20177	22.03157
180	3.72168	4738	3.53505	1105	18.70795	19142	22.24301
190	3.76906	4983	3.54611	1288	18.89937	18220	22.45458
200	3.81890	5157	3.55849	1362	19.08157	17394	22.64007
210	3.87047	5266	3.57212	1475	19.25552	16651	22.82764
220	3.92313	5318	3.58687	1577	19.42203	15978	23.00891
230	3.97632	5323	3.60265	1667	19.58182	15367	23.18447
240	4.02955	5288	3.61933	1746	19.73549	14810	23.35482
250	4.08243	5223	3.63679	1814	19.88359	14298	23.52039
260	4.13467	5133	3.65494	1872	20.02658	13828	23.68153
270	4.18600	5026	3.67366	1919	20.16487	13394	23.83854
280	4.23627	4906	3.69286	1958	20.29882	12992	23.99169
290	4.28534	4778	3.71245	1989	21.42875	12619	24.14120
300	4.33313	4646	3.73235	2013	20.55494	12271	24.28729
310	4.37959	4511	3.75248	2030	20.67765	11945	24.43014
320	4.42471	4378	3.77279	2042	20.79711	11640	24.56990
330	4.46849	4246	3.79321	2048	20.91352	11354	24.70673
340	4.51096	4118	3.81370	2051	21.02706	11084	24.84076
350	4.55215	3995	3.83421	2050	21.13791	10830	24.97212
360	4.59210	3877	3.85471	2045	21.24621	10589	25.10092
370	4.63088	3765	3.87517	2038	21.35210	10361	25.22727
380	4.66853	3658	3.89555	2029	21.45572	10145	25.35127
390	4.70511	3558	3.91584	2017	21.55717	9939	25.47301
400	4.74069	3463	3.93602	19875	21.65656	46933	25.59259
450	4.90553	14768	4.03477	9457	22.12590	43004	26.16068
500	5.05321	13540	4.12935	9022	22.55594	39783	26.68530
550	5.18861	12637	4.21957	8607	22.95378	37087	27.17335
600	5.31499	11936	4.30565	8227	23.32465	34790	27.63030
650	5.43435	11356	4.38792	7883	23.67256	32808	28.06048
700	5.54792	10843	4.46675	7571	24.00064	31077	28.46740
750	5.65636	10368	4.54247	7288	24.31142	29550	28.85389
800	5.76004	9912	4.61535	7027	24.60692	28192	29.22228
850	5.85917	9468	4.68563	6784	24.88885	26975	29.57448
900	5.95386	9032	4.75347	6557	25.15830	25877	29.91208
950	6.04418	8604	4.81905	6342	25.41738	24880	30.23643
1000	6.13022	8184	4.88247	6138	25.66619	23971	30.54866
1050	6.21207	7776	4.94386	5942	25.90590	23136	30.84976
1100	6.28984	7381	5.00328	5755	26.13726	22368	31.14055
1150	6.36365	7000	5.06084	5575	26.36095	21657	31.42179
1200	6.43366	12921	5.11660	10637	26.57752	21079	31.69412
1300	6.56287	11596	5.22297	9692	26.99131	19075	32.21428
1400	6.67883	10409	5.32289	9392	27.38207	17047	32.70496
1500	6.78293	9357	5.41682	8835	27.75255	15244	33.16937
1600	6.87650	8431	5.50518	8318	28.10499	13627	33.61017
1700	6.96081	7617	5.58836	7839	28.44126	12166	34.02963
1800	7.03699	6906	5.66676	7396	28.76231	10838	34.42969
1900	7.10605	6283	5.74073	6986	29.07131	9625	34.81204
2000	7.16888	5737	5.81059	6606	29.36757	8511	35.17816
2100	7.22626	5260	5.87666	6255	29.65268	7483	35.52934
2200	7.27887	4840	5.93921	5931	29.92752	6532	35.86674
2300	7.32727	4472	5.99853	5630	30.19285	5649	36.19138
2400	7.37200	4147	6.05483	5352	30.44935	4826	36.50418
2500	7.41347	3859	6.10836	5094	30.69761	4057	36.80598
2600	7.45207	3605	6.15931	4855	30.93819	3337	37.09750
2700	7.48812	3379	6.20786	4633	31.17156	2660	37.37943
2800	7.52192	3177	6.25420	4426	31.39817	2024	37.65237
2900	7.55370	2998	6.29846	4234	31.61841	1424	37.91688
3000	7.58368	2828	6.34081	7943	31.83266	11179	38.17348
3200	7.63897	5005	6.42025	7318	32.24446	39145	38.66471
3400	7.68902	4577	6.49343	6771	32.63591	37309	39.12935
3600	7.73479	4223	6.56114	6289	33.00901	35644	39.57015
3800	7.77703	3928	6.62404	5864	33.36546	34127	39.98950
4000	7.81631	3680	6.68268	5486	33.70673	32739	40.38442
4200	7.85312	3469	6.73755	5150	34.03412	31463	40.77168
4400	7.88781	3288	6.78905	4849	34.34876	30286	41.13781
4600	7.92069	3132	6.83755	4578	34.65162	29198	41.48917
4800	7.95201	2996	6.88333	4335	34.94360	28187	41.82694
5000	7.98198	-----	6.92669	-----	35.22548	-----	42.15217

TABLE 3. Ideal gas thermodynamic functions for DCN

°K	$\frac{C_p}{R}$		$\frac{(H^\circ - E_0^\circ)}{RT}$		$\frac{-(F^\circ - E_0^\circ)}{RT}$		$\frac{S^\circ}{R}$
50	3.50026	43	3.48845	199	14.48342	63620	17.97188
60	3.50069	187	3.49044	157	15.11963	53817	18.61008
70	3.50256	528	3.49202	160	15.65781	46639	19.14983
80	3.50785	1107	3.49362	213	16.12420	41160	19.61782
90	3.51893	1883	3.49575	318	16.53581	36846	20.03156
100	3.53776	2771	3.49894	471	16.90428	33369	20.40322
110	3.56548	3373	3.50366	662	17.23797	30512	20.74163
120	3.60221	4506	3.51028	875	17.54310	28130	21.05338
130	3.64727	5217	3.51903	1098	17.82440	25117	21.34344
140	3.69944	5779	3.53002	1319	18.08558	22498	21.61560
150	3.75723	6188	3.54321	1529	18.32956	22915	21.87278
160	3.81911	6453	3.55851	1721	18.55871	21624	22.11722
170	3.88365	6591	3.57572	1893	18.77496	20491	22.35068
180	3.94586	6624	3.59466	2042	18.97987	19459	22.57453
190	4.01581	6572	3.61508	2168	19.17476	18587	22.78985
200	4.08153	6455	3.63676	2272	19.36074	17798	22.99751
210	4.14609	6291	3.65949	2355	19.53872	17078	23.19821
220	4.20901	6094	3.68304	2420	19.70950	16425	23.39255
230	4.26995	5876	3.70724	2467	19.87375	15829	23.58100
240	4.32871	5646	3.73192	2507	20.03205	15285	23.76398
250	4.38518	5413	3.75693	2521	20.18490	14784	23.94184
260	4.43932	5183	3.78214	2530	20.33274	14321	24.11489
270	4.49115	4958	3.80745	2531	20.47596	13892	24.28341
280	4.54074	4743	3.83276	2523	20.61488	13493	24.44765
290	4.58817	4539	3.85800	2510	20.74982	13121	24.60782
300	4.63357	4348	3.88310	2491	20.88104	12773	24.76414
310	4.67706	4171	3.90801	2468	21.00877	12446	24.91679
320	4.71877	4006	3.93270	2443	21.13324	12139	25.06594
330	4.75884	3856	3.95713	2415	21.25463	11849	25.21176
340	4.79740	3718	3.98128	2385	21.37312	11575	25.35441
350	4.83459	3593	4.00513	2354	21.48887	11315	25.49401
360	4.87052	3479	4.02868	2322	21.60203	11069	25.63071
370	4.90532	3377	4.05190	2290	21.71273	10836	25.76464
380	4.93909	3284	4.07481	2258	21.82109	10613	25.89590
390	4.97194	3201	4.09739	2226	21.92723	10401	26.02463
400	5.00395	15029	4.11966	10673	22.03125	49146	26.15091
450	5.15425	13906	4.22639	9981	22.52271	45051	26.74911
500	5.29331	13197	4.32620	9396	22.97323	41678	27.29944
550	5.42528	12609	4.42017	8907	23.39001	38845	27.81018
600	5.55198	12195	4.50924	8493	23.77847	36431	28.28771
650	5.67393	11713	4.59417	8133	24.14278	34346	28.73695
700	5.79107	11204	4.67551	7813	24.48924	32525	29.16176
750	5.90311	10666	4.75364	7520	24.81150	30920	29.56515
800	6.00978	10110	4.82885	7246	25.12071	29493	29.94956
850	6.11089	9546	4.90132	6987	25.41565	28214	30.31697
900	6.20635	8986	4.97119	6739	25.69779	27059	30.66899
950	6.29622	8438	5.03859	6501	25.96838	26010	31.00698
1000	6.38060	7909	5.10360	6271	26.22849	25053	31.33210
1050	6.45969	7405	5.16632	6049	26.47903	24174	31.64535
1100	6.53375	6928	5.22681	5834	26.72077	23363	31.94758
1150	6.60304	6480	5.28515	5627	26.95441	22613	32.23956
1200	6.66784	6174	5.34143	5434	27.18054	21918	32.52197
1250	6.72819	5908	5.39568	5252	27.40042	21273	32.79507
1300	6.78407	5670	5.44784	5082	27.61476	20673	33.05847
1350	6.83558	5459	5.49784	4924	27.82407	20113	33.31278
1400	6.88287	5273	5.54568	4776	28.02887	19588	33.55847
1450	6.92588	5111	5.59132	4637	28.22957	19093	33.79507
1500	6.96449	4961	5.63488	4506	28.42657	18623	34.02227
1550	7.00000	4820	5.67638	4382	28.61927	18173	34.24007
1600	7.03251	4689	5.71588	4264	28.80807	17743	34.44887
1650	7.06202	4567	5.75338	4151	28.99327	17328	34.64887
1700	7.08853	4454	5.78888	4043	29.17527	16933	34.84007
1750	7.11204	4349	5.82238	3940	29.35327	16553	35.02227
1800	7.13255	4251	5.85388	3842	29.52727	16183	35.19507
1850	7.15006	4159	5.88338	3749	29.69727	15828	35.35887
1900	7.16457	4072	5.91088	3661	29.86327	15483	35.51387
1950	7.17608	4000	5.93638	3578	30.02527	15148	35.66007
2000	7.18459	3941	5.95988	3500	30.18327	14823	35.79727
2050	7.19010	3886	5.98138	3427	30.33727	14508	35.92547
2100	7.19261	3836	5.99988	3359	30.48727	14203	36.04547
2150	7.19212	3791	6.01538	3296	30.63327	13908	36.15747
2200	7.18863	3750	6.02788	3238	30.77527	13623	36.26147
2250	7.18214	3713	6.03738	3184	30.91327	13348	36.35747
2300	7.17265	3680	6.04388	3134	31.04727	13083	36.44547
2350	7.16016	3650	6.04738	3088	31.17727	12828	36.52547
2400	7.14467	3623	6.04788	3046	31.30327	12583	36.59747
2450	7.12618	3600	6.04538	3008	31.42527	12348	36.66147
2500	7.10469	3579	6.03988	2974	31.54327	12123	36.71747
2550	7.08020	3561	6.03138	2944	31.65727	11908	36.76547
2600	7.05271	3545	6.01988	2918	31.76727	11703	36.80547
2650	7.02222	3531	6.00538	2896	31.87327	11508	36.83747
2700	6.98873	3519	5.98788	2878	31.97527	11323	36.86147
2750	6.95224	3509	5.96738	2864	32.07327	11148	36.87747
2800	6.91275	3500	5.94388	2854	32.16727	10983	36.88547
2850	6.87026	3492	5.91738	2848	32.25727	10828	36.88547
2900	6.82477	3485	5.88788	2846	32.34327	10683	36.87747
2950	6.77628	3479	5.85538	2847	32.42527	10548	36.86147
3000	6.72479	3474	5.81988	2850	32.50327	10423	36.83747
3050	6.67030	3470	5.78138	2856	32.57727	10308	36.80547
3100	6.61281	3467	5.73988	2864	32.64727	10203	36.76547
3150	6.55232	3465	5.69538	2874	32.71327	10108	36.71747
3200	6.48883	3464	5.64788	2886	32.77527	10023	36.66147
3250	6.42234	3464	5.59738	2899	32.83327	9948	36.59747
3300	6.35285	3464	5.54388	2914	32.88727	9883	36.52547
3350	6.28036	3464	5.48738	2930	32.93727	9828	36.44547
3400	6.20487	3464	5.42788	2947	32.98327	9783	36.35747
3450	6.12638	3464	5.36538	2965	33.02527	9748	36.26147
3500	6.04489	3464	5.29988	2984	33.06327	9723	36.15747
3550	5.96040	3464	5.23138	3004	33.09727	9708	36.04547
3600	5.87291	3464	5.15988	3025	33.12727	9703	35.92547
3650	5.78242	3464	5.08538	3047	33.15327	9708	35.79747
3700	5.68893	3464	5.00788	3070	33.17527	9723	35.66147
3750	5.59244	3464	4.92738	3094	33.19327	9748	35.51387
3800	5.49295	3464	4.84388	3119	33.20727	9783	35.35887
3850	5.39046	3464	4.75738	3145	33.21727	9828	35.19507
3900	5.28497	3464	4.66788	3172	33.22327	9883	35.02227
3950	5.17648	3464	4.57538	3200	33.22527	9948	34.84007
4000	5.06499	3464	4.47988	3229	33.22327	10023	34.64887
4050	4.95050	3464	4.38138	3259	33.21727	10108	34.44887
4100	4.83201	3464	4.27988	3290	33.20727	10203	34.24007
4150	4.70952	3464	4.17538	3321	33.19327	10308	34.02227
4200	4.58303	3464	4.06788	3353	33.17527	10423	33.79507
4250	4.45254	3464	3.95738	3386	33.15327	10548	33.55887
4300	4.31805	3464	3.84388	3420	33.12727	10683	33.31278
4350	4.17956	3464	3.72738	3455	33.09727	10828	33.05847
4400	4.03707	3464	3.60788	3491	33.06327	10983	32.79507
4450	3.89058	3464	3.48538	3528	33.02527	11148	32.52547
4500	3.74009	3464	3.35988	3566	32.98327	11323	32.24547
4550	3.58560	3464	3.23138	3604	32.93727	11508	31.95747
4600	3.42811	3464	3.09988	3642	32.88727	11703	31.66147
4650	3.26762	3464	2.96538	3680	32.83327	11908	31.35747
4700	3.10413	3464	2.82788	3718	32.77527	12123	31.04547
4750	2.93764	3464	2.68738	3756	32.71327	12348	30.72547
4800	2.76815	3464	2.54388	3794	32.64727	12583	30.39747
4850	2.59566	3464	2.39738	3832	32.57727	12828	30.06147
4900	2.42017	3464	2.24788	3870	32.50327	13083	29.71747
4950	2.24268	3464	2.09538	3908	32.42527	13348	29.36147
5000	2.06219	3464	1.93988	3946	32.34327	13623	28.99747

TABLE 4. Ideal gas thermodynamic functions for TCN

°K	$\frac{C_p}{R}$		$\frac{(H^\circ - E_0^\circ)}{RT}$		$\frac{-(F^\circ - E_0^\circ)}{RT}$		$\frac{S^\circ}{R}$
50	3.50031	89	3.49015	174	14.69139	63649	18.18154
60	3.50120	345	3.49189	153	15.32789	53839	18.81979
70	3.50466	878	3.49343	188	15.86628	46659	19.35971
80	3.51344	1686	3.49531	286	16.33288	41184	19.82819
90	3.53031	2676	3.49818	446	16.74472	36878	20.24290
100	3.55708	3720	3.50264	656	17.11351	33412	20.61615
110	3.59428	4700	3.50920	898	17.44763	30570	20.95684
120	3.64129	5538	3.51819	1155	17.75334	28204	21.27153
130	3.69667	6195	3.52974	1410	18.03539	25208	21.56513
140	3.75862	6662	3.54384	1651	18.29747	24505	21.84132
150	3.82525	6954	3.56036	1871	18.54252	23036	22.10288
160	3.89479	7093	3.57908	2055	18.77289	21759	22.35197
170	3.96572	7107	3.59973	2230	18.99048	20637	22.59022
180	4.03800	7024	3.62204	2368	19.19686	19646	22.81890
190	4.10704	6870	3.64572	2479	19.39332	18762	23.03905
200	4.17574	6665	3.67051	2565	19.58095	17970	23.25147
210	4.24240	6429	3.69617	2629	19.76065	17255	23.45683
220	4.30670	6174	3.72247	2675	19.93320	16605	23.65568
230	4.36844	5913	3.74922	2704	20.09926	16013	23.84849
240	4.42758	5653	3.77626	2719	20.25940	15470	24.03567
250	4.48411	5399	3.80346	2722	20.41411	14970	24.21757
260	4.53811	5158	3.83068	2716	20.56381	14508	24.39450
270	4.58969	4929	3.85785	2702	20.70858	14079	24.56674
280	4.63899	4717	3.88487	2682	20.84968	13679	24.73456
290	4.68617	4520	3.91169	2657	20.98648	13306	24.89817
300	4.73138	4340	3.93827	2628	21.11954	12956	25.05781
310	4.77478	4176	3.96456	2597	21.24910	12628	25.21366
320	4.81655	4027	3.99053	2564	21.37538	12381	25.36592
330	4.85682	3892	4.01618	2530	21.49857	12027	25.51475
340	4.89574	3771	4.04148	2494	21.61884	11751	25.66033
350	4.93346	3662	4.06643	2459	21.73636	11490	25.80279
360	4.97008	3564	4.09102	2424	21.85126	11242	25.94229
370	5.00572	3476	4.11526	2389	21.96368	11006	26.07895
380	5.04049	3397	4.13916	2354	22.07375	10782	26.21291
390	5.07447	3327	4.16270	2321	22.18157	10568	26.34428
400	5.10774	15795	4.18592	11131	22.28725	49953	26.47317
450	5.26569	14778	4.29723	10430	22.78678	42821	27.08402
500	5.41348	14037	4.40154	9842	23.24500	45417	27.64654
550	5.55385	13388	4.49996	9344	23.66917	39558	28.16914
600	5.68774	12749	4.59341	8912	24.06376	37121	28.65817
650	5.81523	12091	4.68253	8526	24.43597	35015	29.11851
700	5.93615	11414	4.76780	8173	24.78513	33175	29.55393
750	6.05030	10728	4.84953	7843	25.11788	31550	29.96742
800	6.15758	10046	4.92797	7531	25.43339	30103	30.36136
850	6.25805	9380	5.00329	7234	25.73844	28802	30.73771
900	6.35186	8740	5.07563	6949	26.02246	27630	31.09810
950	6.43926	8132	5.14513	6676	26.28676	26562	31.44389
1000	6.52059	7560	5.21189	6414	26.56438	25585	31.77628
1050	6.59620	7026	5.27603	6162	26.82023	24687	32.09627
1100	6.66647	6531	5.33766	5921	27.06711	23858	32.40477
1150	6.73178	6074	5.39687	5690	27.30569	23089	32.70256
1200	6.79253	10920	5.45377	10728	27.53659	44082	32.99037
1300	6.90173	9500	5.56105	9923	27.97742	41579	33.53847
1400	6.99673	8309	5.66028	9192	28.39322	39369	34.05350
1500	7.07982	7312	5.75221	8530	28.78691	37399	34.53913
1600	7.15295	6476	5.83752	7932	29.16091	35630	34.99843
1700	7.21772	5774	5.91684	7390	29.51721	34031	35.43406
1800	7.27546	5181	5.99075	6900	29.85753	32577	35.84828
1900	7.32728	4679	6.05975	6456	30.18330	31248	36.24306
2000	7.37407	4251	6.12431	6054	30.49579	30028	36.62011
2100	7.41659	3886	6.18485	5688	30.79607	28904	36.98093
2200	7.45545	3572	6.24174	5355	31.08512	27865	37.32686
2300	7.49118	3301	6.29530	5052	31.36377	26900	37.65907
2400	7.52419	3066	6.34582	4775	31.63277	26002	37.97860
2500	7.55485	2861	6.39358	4522	31.89280	25164	38.28638
2600	7.58347	2682	6.43880	4289	32.14445	24381	38.58325
2700	7.61030	2525	6.48169	4076	32.38826	23646	38.86996
2800	7.63555	2386	6.52246	3879	32.62473	22956	39.14719
2900	7.65941	2263	6.56125	3698	32.85430	22306	39.41556
3000	7.68205	4209	6.59824	6907	33.07737	21697	39.67561
3200	7.72414	3858	6.66731	6331	33.50544	40613	40.17276
3400	7.76273	3572	6.73063	5834	33.91157	38638	40.62221
3600	7.79845	3338	6.78897	5401	34.29796	36852	41.08694
3800	7.83183	3142	6.84299	5023	34.66648	35229	41.50948
4000	7.86326	2978	6.89233	4690	35.01878	33746	41.91201
4200	7.89304	2837	6.94013	4396	35.35625	32388	42.29639
4400	7.92142	2717	6.98410	4134	35.68013	31137	42.66423
4600	7.94859	2612	7.02545	3901	35.99151	29983	43.01696
4800	7.97471	2520	7.06446	3691	36.29134	28914	43.35580
5000	7.99991	-----	7.10138	-----	36.58048	-----	43.68186



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